

Handwritten HW 35

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12. Find a polynomial p_3 such that $\{p_0, p_1, p_2, p_3\}$ (see Exercise 11) is an orthogonal basis for the subspace \mathbb{P}_3 of \mathbb{P}_4 . Scale the polynomial p_3 so that its vector of values is $(-1, 2, 0, -2, 1)$.

Solution:

Exercise 11 says, “Let p_0 , p_1 , and p_2 be the orthogonal polynomials described in Example 5, where the inner product on \mathbb{P}_4 is given by evaluation at -2 , -1 , 0 , 1 , and 2 .”

32. Let V be the space $C[-2, 2]$ with the inner product of Example 7. Find an orthogonal basis for the subspace spanned by the polynomials 1 , t , and t^2 .

Solution: